



MODELING OF NEW HIGH VOLTAGE POWER SUPPLY WITH THREE-PHASE CHARACTER FOR MICROWAVES GENERATORS WITH ONE MAGNETRON BY PHASE UNDER MATLAB SIMULINK CODE

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ABSTRACT

This original work treats the modeling of the new model of three-phase high voltage power supply for microwaves generators with one magnetron by phase under MATLAB SIMULINK code. The design of this system is composed of new three-phase transformer supplying by phase a cell doublers composed of a capacitor and a diode. Each cell in turn, supplies a single magnetron. The modeling of this new model of power supply passes obligatorily by the modeling and dimensioning of its own three-phase transformer with magnetic shunt which ensures the stabilization of the anodic current in each magnetron. This model was tested with the help of MATLAB SIMULINK code. The electrical signal obtained (voltages and currents) are curves of various sizes, periodic, non-sinusoidal and dephasing by $(2\pi/3)$ between them. These signals have the same form as those of experimental and simulated of conventional power supply using a single phase transformer for one magnetron.

Keywords: microwaves, modeling, MATLAB SIMULINK, Three-phase transformer, high voltage, magnetron.

1. INTRODUCTION

Currently to supply one magnetron, the current single-phase power supply actually manufactured at the manufacturer of the power supply for magnetrons uses a single-phase transformer with magnetic shunt powering a cell doublers composed of a diode and a capacitor and one magnetron at the output of the cell. Based on the encouraging results obtained from the modeling of a new generation of single-phase HV power supplies for industrial microwaves generators with several magnetrons [1-16], this original work aims to develop a new model of high voltage power supply with a three-phase character for microwaves generators with one magnetron by phase. This will contribute to the development of the technological innovation in the manufacturing industry of the power supply for magnetron of microwave ovens for domestic or industrial use.

The modeling of this new model of three-phase power supply for one magnetron passes necessarily by the modeling and the dimensioning of its own high voltage three-phase transformer, which ensures the stabilization of the average anodic current in each magnetron. In our design of this new three-phase transformer with magnetic shunts, we use an armored structure tetrahedron type (Figure-1) to represent the equivalent magnetic circuit of the transformer, which will undoubtedly allow to reduce the congestion and the volume of this new device and makes it more economical. Therefore it ensures lower cost of implementation and maintenance of microwave generators. It is for this reason that the new design is more advantageous than the combination of three identical single-phase models connected in star.

In this paper we will implement and validate this model under MATLAB-SIMULINK. It is a π quadruple [17, 18, 19] model derived from diagram of the armored structure magnetic circuit tetrahedron type equivalent of the new three phase transformer with magnetic shunts. This model is composed of storable inductances able to translating the nonlinear saturation phenomena. The results obtained from this simulation compared with those obtained by experimental and simulated of conventional power supply using a single phase transformer for one magnetron are in good conformity.

2. PRINCIPLE OF MODELING

The new three-phase transformer with magnetic shunts for the new high voltage power supply uses an armored structure tetrahedron type (Figure-1) to represent its equivalent magnetic circuit. A magnetic shunt serves to divert an important part of flux circulating between the primary and secondary windings of each phase. The primary and secondary fluxes of the three phase respectively, are added together to cross the common reluctances R_{COM} and R_{com} . Other hand, taking into account the air-gaps dimension and the magnetic state of saturation, the magnetic fluxes of air dispersion are negligible compared to one through the shunts. Hereafter, we consider the new three-phase transformer without iron losses (hysteresis loss and eddy current). And to simplify the study, we consider the Star Star (Yy) coupling between the primary and secondary windings.

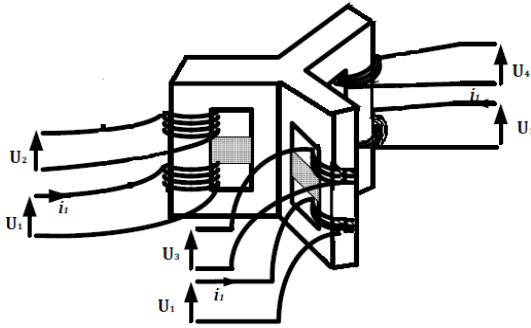


Figure-1. Form of the new three-phase transformer with magnetic shunt.

2.1. Mathematical equations and dimensioning

The primary quantities are represented by a capital letter and the secondary quantities are represented by a lowercase letter:

- $r_A, r_B, r_C, r_a, r_b, r_c$: represent the primary and secondary resistances of phases A, B, C.
- $i_A, i_B, i_C, i_a, i_b, i_c$: represent the currents traversing the primary and secondary windings of phases A, B, C.
- $U_A, U_B, U_C, u_a, u_b, u_c$: are the primary and secondary windings voltages of phases A, B, C.
- $\Phi_A, \Phi_B, \Phi_C, \Phi_a, \Phi_b, \Phi_c, \Phi_{sh}$: represent the primary, secondary and shunts fluxes by turn in each phase.
- n_1, n_2 : the number of primary and secondary turns for each phase.
- $R_A, R_B, R_C, R_a, R_b, R_c, R_{sh}$: magnetic circuit reluctances of primary, secondary and shunts of each phase, traversed respectively by the fluxes $\Phi_A, \Phi_B, \Phi_C, \Phi_a, \Phi_b, \Phi_c, \Phi_{sh}$.

R_{COM} and R_{com} : represent the common reluctances between the three phases traversed by the common flux Φ_{COM} and Φ_{com}

❖ Electrical equations

By the application of Ohm's generalized law to the primary windings (receiver convention) and secondary ones (generator convention), we obtain the six electrical equations governing the operating of the three-phase transformer.

- For the phase A:

$$U_A = r_A i_A + n_1 \cdot \frac{\partial \Phi_A}{\partial t} \quad (1)$$

$$U_a = -r_a i_a + n_2 \cdot \frac{\partial \Phi_a}{\partial t} \quad (2)$$

- For the phase B:

$$U_B = r_B i_B + n_1 \cdot \frac{\partial \Phi_B}{\partial t} \quad (3)$$

$$U_b = -r_b i_b + n_2 \cdot \frac{\partial \Phi_b}{\partial t} \quad (4)$$

- For the phase C:

$$U_C = r_C i_C + n_1 \cdot \frac{\partial \Phi_C}{\partial t} \quad (5)$$

$$U_c = -r_c i_c + n_2 \cdot \frac{\partial \Phi_c}{\partial t} \quad (6)$$

By writing each total flux in the form: $n \cdot \Phi = L i$, the previous equations become:

$$U_A = r_A i_A + n_1 \cdot \frac{\partial}{\partial t} (L_A i_A) \quad (7)$$

$$U_a = -r_a i_a + n_2 \cdot \frac{\partial}{\partial t} (l_a i_a) \quad (8)$$

$$U_B = r_B i_B + n_1 \cdot \frac{\partial}{\partial t} (L_B i_B) \quad (9)$$

$$U_b = -r_b i_b + n_2 \cdot \frac{\partial}{\partial t} (l_b i_b) \quad (10)$$

$$U_C = r_C i_C + n_1 \cdot \frac{\partial}{\partial t} (L_C i_C) \quad (11)$$

$$U_c = -r_c i_c + n_2 \cdot \frac{\partial}{\partial t} (l_c i_c) \quad (12)$$

❖ Magnetic equations

From the diagram of the equivalent magnetic circuit of the new three-phase transformer with shunts (Figure-2) and by applying the Hopkinson's law, we can write the magnetic equations for each phase of the new three-phase transformer with magnetic shunts.

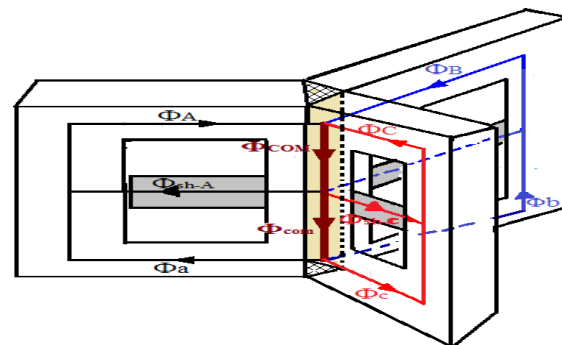


Figure-2. Magnetic circuit of type tetrahedron of the new three-phase transformer with magnetic shunts.



We take the phase A as example:

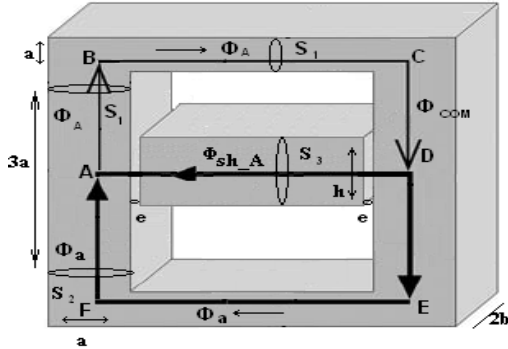


Figure-3. Diagram of the equivalent magnetic circuit of the new transformer (Phase A as example).

- for the ride ABCDA:

$$(R_{AB} + R_{BC})\Phi_A + R_{CD}\Phi_{COM} + R_{AD}\Phi_{sh-A} = n_1 i_A$$

By posing:

$$R_A = (R_{AB} + R_{BC}), R_{COM} = R_{CD}, R_{sh-A} = R_{DA}$$

The previous equation becomes:

$$R_A \Phi_A + R_{COM} \Phi_{COM} + R_{sh-A} \Phi_{sh-A} = n_1 i_A \quad (13)$$

- for the ride ADEFA:

$$-R_{AD}\Phi_{sh-A} + (R_{EE} + R_{FA})\Phi_a + R_{DE}\Phi_{com} = -n_2 i_a$$

By posing: $R_a = (R_{EE} + R_{FA}), R_{com} = R_{DE}$

The previous equation becomes:

$$-R_{sh-A}\Phi_{sh-A} + R_a\Phi_a + R_{com}\Phi_{com} = -n_2 i_a \quad (14)$$

- for the ride BCEFA:

$$R_A\Phi_A + R_{COM}\Phi_{COM} + R_a\Phi_a + R_{com}\Phi_{com} = n_1 i_A - n_2 i_a \quad (15)$$

In balanced three-phase system the fluxes $\Phi_{\square\square\square}$ (the flow through the central core of primary side) and $\Phi_{\square\square\square}$ (the flow through the central core of secondary side) are considered zero because they are the composition of three balanced flow.

$$\Phi_{COM} = \Phi_A + \Phi_B + \Phi_C = 0 \quad (16)$$

$$\Phi_{com} = \Phi_a + \Phi_b + \Phi_c = 0 \quad (17)$$

So the previous equations become:

$$R_A \Phi_A + R_{sh-A} \Phi_{sh-A} = n_1 i_A \quad (18)$$

$$-R_{sh-A} \Phi_{sh-A} + R_a \Phi_a = -n_2 i_a \quad (19)$$

$$R_A \Phi_A + R_a \Phi_a = n_1 i_A - n_2 i_a \quad (20)$$

The Equations (18) to (20) are supplemented by additional relationships reflecting the law of conservation of flux per phase.

$$\Phi_A = \Phi_a + \Phi_{sh-A} \quad (21)$$

$$\Phi_B = \Phi_b + \Phi_{sh-B} \quad (22)$$

$$\Phi_C = \Phi_c + \Phi_{sh-C} \quad (23)$$

2.2. Equivalent scheme of the new transformer

We take always the phase A as example:

$$U_A = r_A i_A + n_1 \frac{\partial \Phi_A}{\partial t} \quad (24)$$

$$U_a = -r_a i_a + n_2 \frac{\partial \Phi_a}{\partial t} \quad (25)$$

Multiplying the equation (24) by (n_2/n_1) and writing the quantity $(n_1 \cdot \Phi_A)$

as $(n_1 \cdot \Phi_A = n_1 (\frac{n_2}{R_A}) (\frac{R_A}{n_2}) \Phi_A)$, we obtain:

$$U'_A = r'_A i'_A + n_2 \frac{\partial \Phi_A}{\partial t} \\ = r'_A i'_A + \frac{\partial}{\partial t} \left(\frac{n_2^2}{R_A} \Phi_A \right)$$

With: $(U'_A = \frac{n_2}{n_1} U_A)$, $(r'_A = (\frac{n_2}{n_1})^2 r_A)$ and $(i'_A = \frac{n_1}{n_2} i_A)$

By posing the inductance $(L'_{p-A} = \frac{n_2^2}{R_A})$ and the electric

current $(i'_{p-A} = \frac{R_A \Phi_A}{n_2})$. The previous equation becomes:

$$U'_A = r'_A i'_A + \frac{\partial}{\partial t} (L'_{p-A} i'_{p-A}) \quad (26)$$

We replace $n_2 \Phi_a$ in the equation (25) by

$(n_2 \Phi_a = \frac{n_2^2}{R_a} \frac{R_a}{n_2} \Phi_a)$ and by posing the inductance

$(L'_{s-a} = \frac{n_2^2}{R_a})$ and the electric current $i'_{s-a} = \frac{R_a \Phi_a}{n_2}$ we

obtain:



$$U_a = -r_a i_a + \frac{\partial}{\partial t} (L_{s-a} i_{s-a}) \quad (27)$$

Using the equation (21) and writing the value $n_2 \cdot \Phi_a$ in the form $(n_2 \cdot \Phi_a = \frac{n_2^2}{R_a} \cdot \frac{R_a}{n_2} \cdot \Phi_a)$ and the value $n_2 \cdot \Phi_{sh-A}$ as $(n_2 \cdot \Phi_{sh-A} = \frac{n_2^2}{R_{sh-A}} \cdot \frac{R_{sh-A}}{n_2} \cdot \Phi_{sh-A})$. The development of the auto-induction force expression $n_2 \cdot \frac{\partial \Phi_A}{\partial t}$ can lead to the following relation:

$$n_2 \cdot \frac{\partial \Phi_A}{\partial t} = \frac{\partial}{\partial t} \left(\frac{n_2^2}{R_a} \right) \left(\frac{R_a \cdot \Phi_a}{n_2} \right) + \frac{\partial}{\partial t} \left(\frac{n_2^2}{R_{sh-A}} \right) \left(\frac{R_{sh-A} \cdot \Phi_{sh-A}}{n_2} \right)$$

By posing $(L'_{sh-A} = \frac{n_2^2}{R_{sh-A}})$ and the current

$$(i'_{sh-A} = \frac{R_{sh-A} \cdot \Phi_{sh-A}}{n_2}) \text{ the previous equation becomes:}$$

$$n_2 \cdot \frac{\partial \Phi_A}{\partial t} = \frac{\partial}{\partial t} (L_{s-a} i_{s-a}) + \frac{\partial}{\partial t} (L'_{sh-A} i'_{sh-A}) \quad (28)$$

Using the equations (18) and (19) we can arrive at the expressions:

$$\frac{n_1}{n_2} i_A = \frac{R_A \Phi_A}{n_2} + \frac{R_{sh-A} \cdot \Phi_{sh-A}}{n_2}$$

$$i_a = \frac{-R_{sh-A} \cdot \Phi_{sh-A}}{n_2} + \frac{R_a \cdot \Phi_a}{n_2}$$

These expressions can be written in the form:

$$i'_A = i'_{p-A} + i'_{sh-A} \quad (29)$$

$$i_{s-a} = i'_{sh-A} + i_a \quad (30)$$

The equations (26) to (30) respond to equivalent circuit referred to secondary for the first phase of the new three-phase transformer with magnetic shunts (Figure-4). Everything happens as if each phase of the three-phase HV transformer with magnetic shunts is composed of three ideal transformers; each one supplying a quadruple π composed of three inductive elements L'_{p-A} on the primary side, L_{s-a} on the secondary side and L'_{sh-A} on the shunts side.

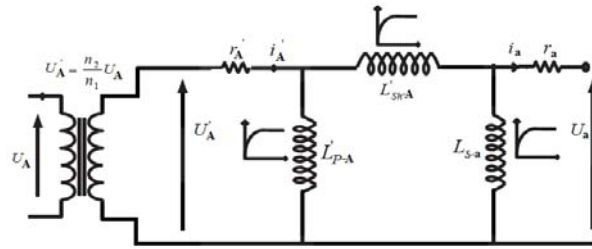


Figure-4. Quadruple model of storable inductances referred to secondary equivalent of new three-phase transformer with magnetic shunts.

According to the model established the reluctance R_{sh-A} is the reluctance corresponding to the path DA (Figure-2). It corresponds to the reluctance of the ferromagnetic part $(R_{sh-A})^f$ and the reluctance constant $(R_{sh-A})^e$ caused by the air of the air gap, hence:

$$R_{sh-A} = (R_{sh-A})^f + (R_{sh-A})^e \quad (31)$$

$$\text{With: } (R_{sh-A})^f = \frac{l_{sh-A} - 2 \cdot e}{\mu \cdot S3} \text{ and } (R_{sh-A})^e = \frac{2 \cdot e}{\mu_0 \cdot S3}$$

By writing the expression of the L'_{sh-A} according to $(R_{sh-A})^f$ and $(R_{sh-A})^e$, it comes:

$$L'_{sh-A} = \frac{n_2^2}{(R_{sh-A})^f + (R_{sh-A})^e} = \frac{\frac{n_2^2}{(R_{sh-A})^f} * \frac{n_2^2}{(R_{sh-A})^e}}{\frac{n_2^2}{(R_{sh-A})^f} + \frac{n_2^2}{(R_{sh-A})^e}}$$

By posing:

$$(L'_{sh-A})^f = \frac{n_2^2}{(R_{sh-A})^f} \text{ and } (L'_{sh-A})^e = \frac{n_2^2}{(R_{sh-A})^e}$$

We obtain thus:

$$L'_{sh-A} = \frac{(L'_{sh-A})^f * (L'_{sh-A})^e}{(L'_{sh-A})^f + (L'_{sh-A})^e} \quad (32)$$

We know that the inductance

$$L'_{sh-A} = \frac{n_2^2}{(R_{sh-A})} \text{ covered by the current } i'_{sh-A} \text{ obeys the}$$

$$\text{law: } (n_2 \cdot \Phi_{sh-A} = L'_{sh-A} \cdot \Phi_{sh-A})$$

Other hand, the current expression i'_{sh-A} becomes:

$$i'_{sh-A} = \frac{R_{sh-A} * \Phi_{sh-A}}{n_2} = \frac{(R_{sh-A})^f * \Phi_{sh-A}}{n_2} + \frac{(R_{sh-A})^e * \Phi_{sh-A}}{n_2}$$

by posing:

$$(i'_{sh-A})^f = \frac{(R_{sh-A})^f * \Phi_{sh-A}}{n_2} \quad (i'_{sh-A})^e = \frac{(R_{sh-A})^e * \Phi_{sh-A}}{n_2}$$

We obtain thus:



$$n_2 \cdot \Phi_{sh-A} = (L'_{sh-A})^f * (i'_{sh-A})^f + (L'_{sh-A})^e * (i'_{sh-A})^e \quad (33)$$

From equations (31), (32) and (33), we find thus that the inductance L'_{sh-A} is equivalent to two inductances $(L'_{sh-A})^e$ and $(L'_{sh-A})^f$ in parallel. The π quadruple model of the three phase transformer with shunts in Figure-3 is slightly modified, it becomes equivalent to that of Figure-5.

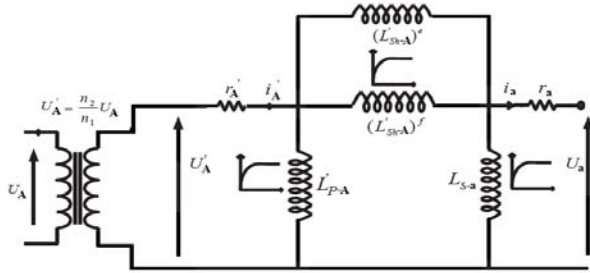


Figure-5. New quadruple model of three-phase transformer with shunts.

By perfectly similar calculations, the equation system which responds to the equivalent diagram of the phase B and C permits to find the models indicated on the Figure-6.

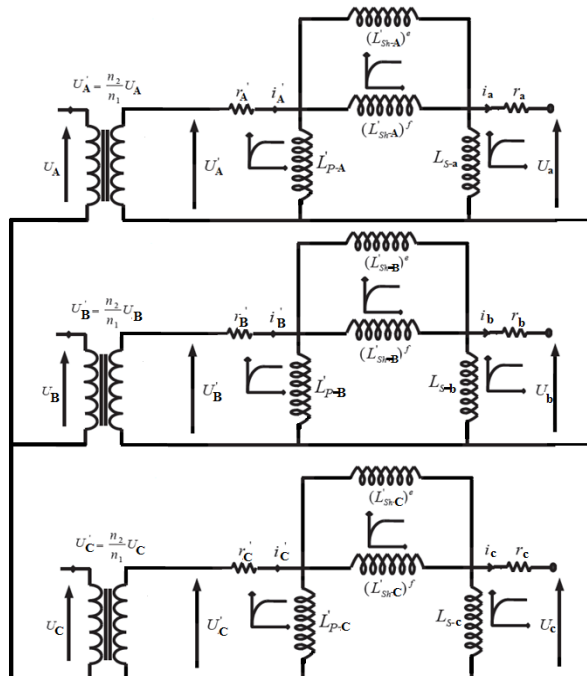


Figure-6. New model of the new three-phase transformer with magnetic shunts.

In perfect transformer input of phases A, B, C, we have the currents i_A , i_B , i_C and the voltages U_A , U_B , and U_C . And in its outputs, we find the voltages $U'_A = (n_2/n_1)U_A$, $U'_B = (n_2/n_1)U_B$ and $U'_C = (n_2/n_1)U_C$ and the currents

$i'_A = (n_1/n_2) \cdot i_A$, $i'_B = (n_1/n_2) \cdot i_B$ and $i'_C = (n_1/n_2) \cdot i_C$. Finally we obtain to the output terminals of these quadruples the real voltage of output of three-phase transformer with shunt u_a, u_b, u_c .

3. VALIDATION OF THE NEW MODEL OF THE NEW POWER SUPPLY UNDER MATLAB SIMULINK

3.1. Simulation with Matlab - Simulink the nominal functioning of the new three-phase power supply

the model of the new transformer is integrated in the new High voltage power supply circuit from the source to the magnetrons (Figure-8). Each magnetron is represented by an equivalent diagram deduced from its electrical characteristics which is formally similar to that of a diode with dynamic resistance $R=350$ Ohms and threshold voltage $E=3800$ Volts.

The nonlinear inductors [20, 21] studied in Figure-6 depend on the reluctance of the magnetic circuit portion with a section S and average length l . Each one is represented by its characteristic $\Phi(i)$ derived from the relation $L(i) = (n^2 \Phi(i) / i)$ determined from the magnetization curve $B(H)$ of the material used and the geometrical dimensions of the transformer. A specific routine was developed in MATLAB to derive the pair of values (i, Φ) from those (H, B) and geometric data for the three inductors using the relation: $\Phi(i) = n^2 \cdot B \cdot S$ and $i = (H \cdot l) / n^2$.

- For the primary inductance L'_{p-A} :

$$i'_{p-A} = \frac{l_p}{n_2} * H, \Phi_A = n_2 * B * S_1$$

- For the secondary inductance L_{s-a} :

$$i_a = \frac{l_s}{n_2} * H, \Phi_a = n_2 * B * S_2$$

- For the shunt inductance L'_{sh-a} :

$$i_{sh-A} = \frac{l_{sh}}{n_2} * H, \Phi_{sh-A} = n_2 * B * S_3$$

The implementation of each nonlinear inductance in MATLAB-SIMULINK code was performed using the following blocks (Figure-7):

- An integrator to convert the voltage in flow.
- A (lookup table $i = \Phi(i)$) function, which accepts a large number of N points relating to the currents.
- An imposed current source

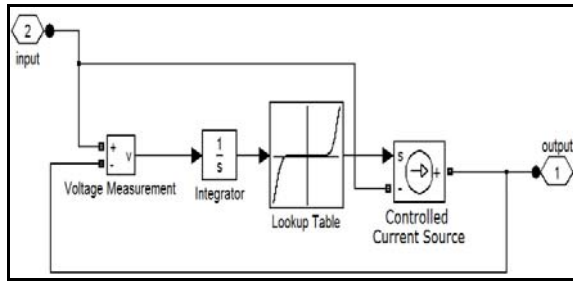


Figure-7. Diagram block of one non-linear inductance.

Each inductor of the Figure-6 is replaced by its equivalent block, and then we introduce them in the overall scheme of the new three-phase power supply with one magnetron by phase to be suitable for the modeling of the whole device (Figure-8).

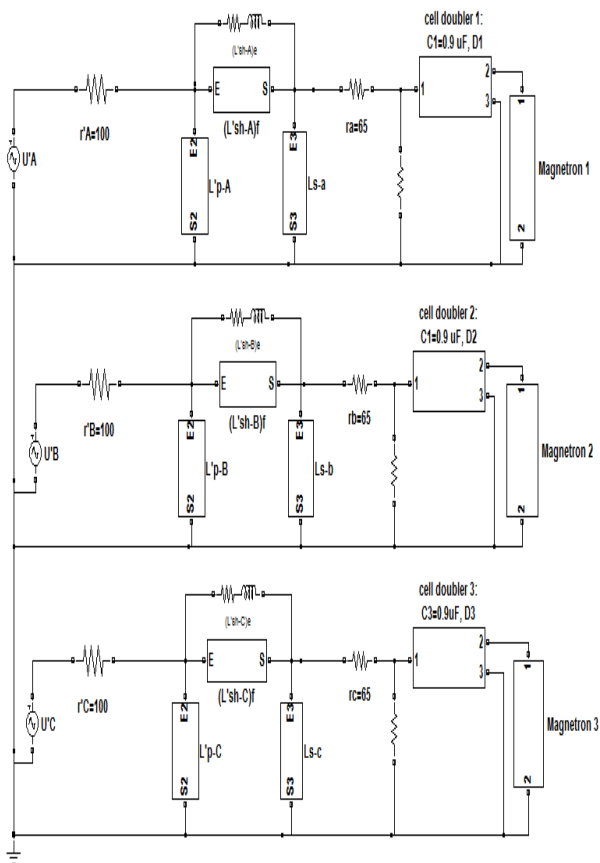


Figure-8. Diagram of the three-phase power supply simulated with MATLAB SIMULINK (one magnetron by phase).

We validate this model by comparing simulation results with those obtained from tests already carried out [2]-[17] of conventional power supply using a single phase transformer for one magnetron.

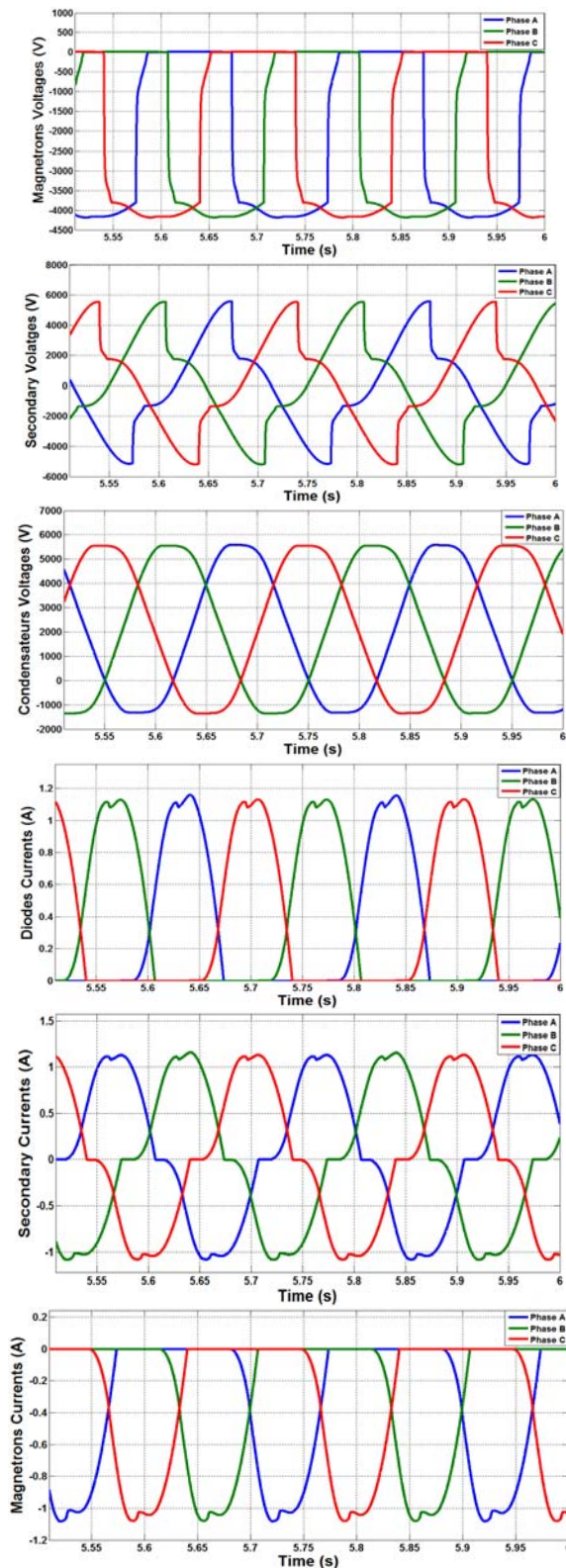


Figure-9. Simulation with MATLAB SIMULINK: Forms of currents and voltages waves.



Experimental setup and results

The Figure-10 shows the experimental setup for measuring the characteristics current and voltage of the high voltage power supply for magnetron in nominal operation. This test was performed in the department of electrical engineering of higher School of Technology in Agadir (Marocco).

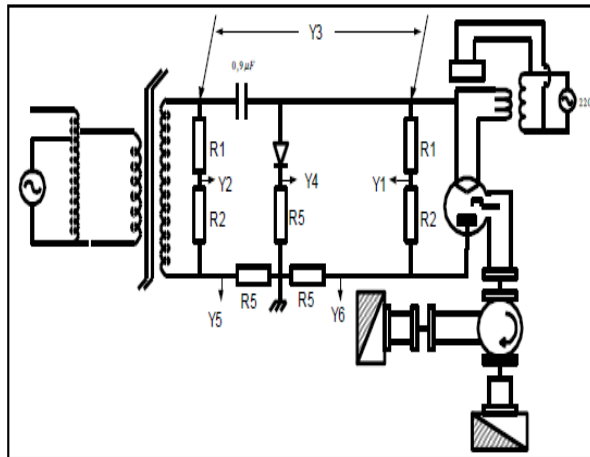


Figure-10. Experimental set up for measuring of the characteristics: current and voltage of the power supply HV for magnetron innominal operation.

Y1 : magnetron voltage,
Y2 : secondary voltage,
Y3 : condansator voltage,
Y4 : diode current,
Y5 : secondary current,
Y6 : magnetron current,
R1= 10MΩ, R2=10 KΩ, R3=22 Ω

To validate this model, we performed a test on a microwave generators composed of the following elements:

- High voltage transformer with magnetic shunts possesses the nominal characteristics : $f=50$ Hz, $S=1650$ VA, $U_1=220$ V, and vacuum $U_2=2330$ V
- Primary resistance referred to secondary $r_1'=100$ Ω, secondary resistance $r_2=65$ Ω.
- Number of turns in primary $n_1=224$, number of turns in secondary $n_2 = 2400$.
- A capacitor $C = 0.9$ μF and a high-voltage diode DHT.
- A magnetron designed to function under a voltage approximately 4000 V. To obtain its nominal power, it needs an average current $I_{mean}=300$ mA, but without exceeding the peak current which might destroy it ($I_{peak} < 1, 2$ A).

The experimental curves are presented in Figure-11. The first three curves represent the shapes of voltage quantities while the last ones represent current patterns;

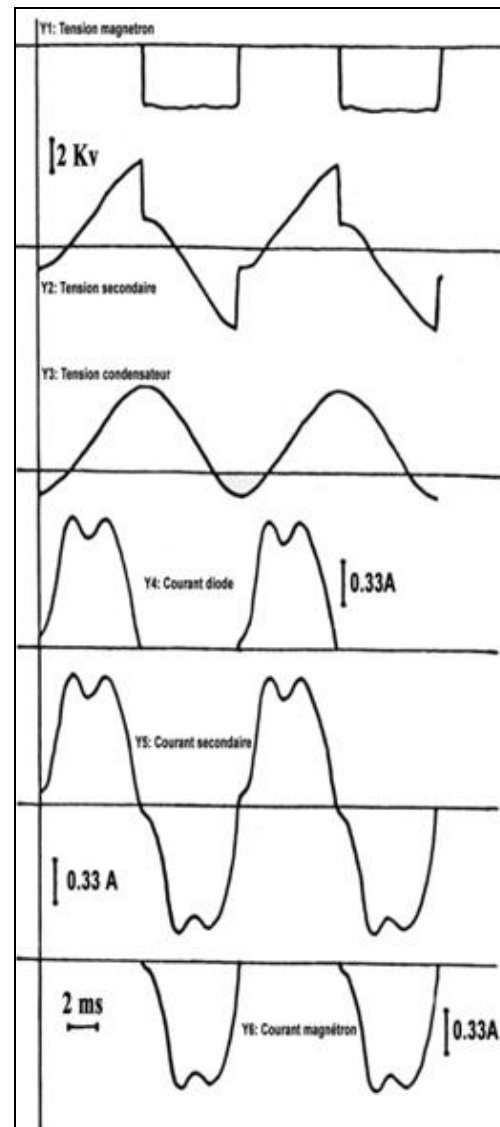


Figure-11. Experimental waveforms of currents and voltages of conventional power supply using a single phase transformer for one magnetron (Nominal state)

The electrical signal obtained (voltages and currents) from simulation with MATLAB SIMULINK are curves of various sizes, periodic, non-sinusoidal and dephasing by $(2\pi/3)$ between them. These signals have the same form as those of experimental and simulated of conventional power supply using a single phase transformer for one magnetron, in particular, the maximum value of the magnetron current which respect the constraint imposed by the manufacturer ($I_{max} < 1.2$ A).

Based on encouraged result obtained previously, the new form of our three-phase transformer becomes that shown in Figure-12. The fluxes $\Phi_{COM} = \Phi_A + \Phi_B + \Phi_C$ (the flow through the central core of primary side) and $\Phi_{com} = \Phi_a + \Phi_b + \Phi_c$ (the flow through the central core



of secondary side) are considered zero, because they are the composition of three balanced flow. So this central core is therefore not necessary. This leads to reducing the volume of the transformer and the weight and the cost of the entire system of the high voltage power supply. This new three-phase transformer present a minimum volume compared to the one already studied [22, 23].

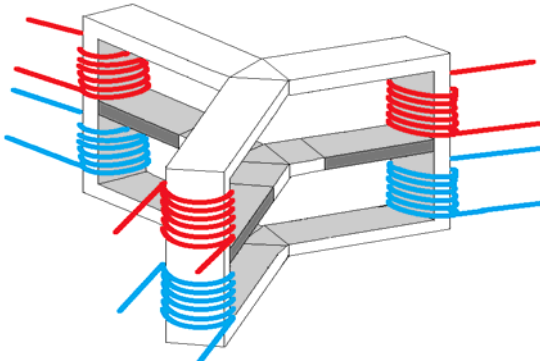


Figure-12. New type of magnetic circuit of the new three-phase transformer with magnetic shunt.

CONCLUSIONS

The modeling of a new model of high voltage power with a three-phase character supplying one magnetron by phase has been inconclusive. It can be extended without any problem in case of new three-phase or six-phase power supply for several magnetrons by phase.

For industrial applications, this modeling of the new three-phase power supply for one magnetron by phase; will certainly encourage us to realize the new three-phase transformer with magnetic shunts for a new generation of industrial microwaves generators. This will contribute to the technological innovation.

As perspectives, an optimization strategy can also be defined using MATLAB SIMULINK code, to reduce the volume of the three-phase transformer and the weight and the cost of the entire system of the high voltage power supply.

APPENDIX

■ Geometry of transformer with magnetic shunts

The distribution of primary, secondary and shunts fluxes in each phase, is the same as that one of single-phase HV transformer with shunts. This leads us to deduce the geometry of the magnetic circuit of the new three-phase transformer from that of single-phase transformer with magnetic shunts.

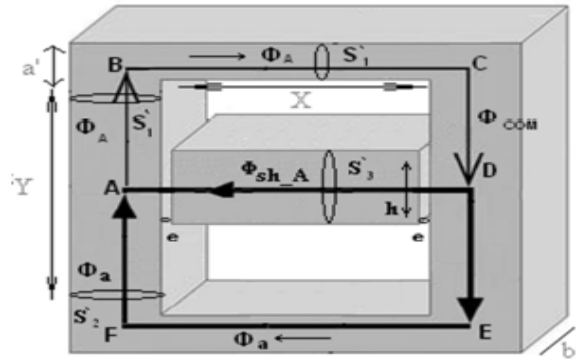


Figure-13. Geometry of transformer with magnetic shunts.

The section $S'1$ must be equal to the section of single-phase transformer with magnetic shunts S_1 :

- $S'_1 = a' \cdot b'$
- $S_1 = 2 \cdot a \cdot b$

Thus, we have two solutions for the geometry of this new three phase transformer with shunts:

- $a' = a$ and $b' = 2 \cdot b$
- $a' = 2 \cdot a$ and $b' = b$

As the section $S'3$ must be the double of the section S_3 .

- $S'_3 = h' \cdot b'$
- $S_3 = h \cdot b$
- $S'_3 = 2 \cdot S_3$

From previous relationships we find that the solution: $a' = a = 25$ mm and $b' = b \cdot 2 = 120$ mm is more realizable

■ Determination of X and Y calculated from the reluctances:

The primary and shunts reluctances that correspond to paths respectively ABCD and AD must therefore be equal to those in case of single phase. That allows us to obtain the system of equations:

- $\frac{1}{2}Y + \frac{1}{2} \cdot a + \frac{1}{2} \cdot a + X + \frac{1}{2}a + \frac{1}{2}a + \frac{1}{2}Y = 6.5 \cdot a$
- $\frac{1}{2} \cdot a + X + \frac{1}{2} \cdot a - 2 \cdot e = 2.5 \cdot a - 2 \cdot e$

From the previous equation we obtain:

- $X = 1.5 \cdot a$
- $Y = 3 \cdot a$

Thus we obtain the following geometrical dimensions of the new three-phase transformer with magnetic shunts:



- The width of the non-wound core: $a = 25$ mm
- The width of the magnetic circuit: $b = 120$ mm
- Number of stacked sheets of the shunt: $n_3 = 18$
- Number of turns in the primary: $n_1 = 224$
- Number of secondary turns: $n_2 = 2400$
- Height of the sheet stack of shunts: $h = 0.5 * n_3$ mm
- Surface of the core: $S_1 = S_2 = a * b$
- Surface of shunt: $S_3 = b * h$
- Thickness of the air gap: $e = 0.75$ mm
- $L_p = 4.5 * a$ (correspond to the path ABC)
- $L_s = 4.5 * a$ (correspond to the path AFE)
- $L_{sh} = 2.5 * a - 2 * e$ (correspond to the path AD)

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