



## AN EFFICIENT LIVER SEGMENTATION USING KERNEL SPARSE CODING AUTOMATED (KSCA) APPROACH

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### ABSTRACT

Computed Tomography (CT) images have been widely used for diagnosis of liver disease and volume measurement for liver surgery or transplantation. The approach is presented with respect to liver segmentation, but it can be easily extended to any other soft tissue by setting appropriately the values of the parameters for the splitting and merging algorithm and for the region growing refinement step. Sparse coding with data-adapted dictionaries has been successfully employed in several image recovery and vision problems. A novel, automated segmentation technique for detecting affected region in liver was proposed in this paper. In the new approach, we constructed ensemble kernel matrices using the pixel intensities and their spatial locations, and obtained kernel dictionaries for sparse coding pixels in a non-linear feature space. The resulting sparse codes were used to train an Extreme Learning Machine (ELM) classifier that determines if a pixel in the image belongs to an affected region. From the experimental results using ten test datasets distributed for the competition, it was confirmed that our method kernel sparse coding based liver segmentation performs better than previous methods or models.

**Keywords:** liver disease, segmentation, auto-context model (ACM), kernel sparse coding automated approach, ELM.

### INTRODUCTION

In recent years, medical image segmentation has become an active area of research and it attracts more and more researchers for novel innovations. Image segmentation automatically explores the internal structures of the patient, which may be anatomical (organs) and pathological (lesions). Automatic segmentation of lesions in a large image database has attracted the attention of several researchers as it assists in diagnosis [1], by identifying possibly forgotten lesions, and also to speed up the process of analysis. Liver is one of the most important organs of the human body. When it is affected by a tumoral pathology, it is possible to operate it by cutting the damaged portion. But the segmentation has to be done with the rules of volumetric and very specific vascularization. The medical imaging is then used to detect and visualize the internal structures. These structures do not appear in a single image, but need several acquisitions which will therefore be compared. The tumoral or hepatic volumetric is possible only after a period of segmentation of these images. Liver analysis plays a vital role in the therapeutic strategy for hepatic diseases. Therefore, the automatic segmentation of the liver has influenced a number of researchers with its importance and it assists in diagnosis of liver diseases such as steatosis, fibrosis, etc. Segmentation of a liver from a three dimensional CT volume serves as the initial process in image-based hepatic investigations [2, 3]. Even though a number of techniques have been developed and available in the literature, fully automatic liver segmentation from a 3D volume is still a challenging factor due to the large variations in liver shapes and in the intensity pattern inside and along liver boundaries.

The main aim of the present research work is to develop a novel approach for automatic liver segmentation

to obtain its internal structures and tumors in a more efficient manner. Auto-Context Model (ACM) has been used in the automatic liver segmentation approach. The present research work extends the approach of Hongwei Ji in [14] which used the ACM model for segmentation. The present research work uses kernel Sparse Coding Automated approach for liver segmentation which overcomes the limitations in ACM approach.

### PREVIOUS WORKS

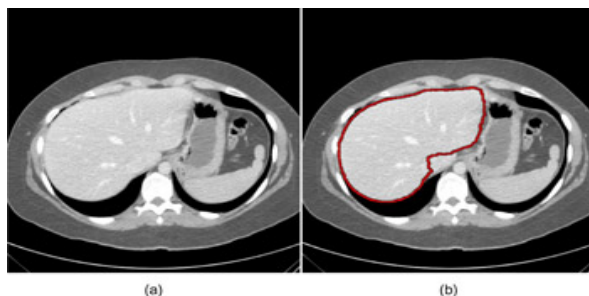
Max-Flow/Min-Cut method [4] this approach is a semi-automatic segmentation of the liver depending on graph theory and more particularly on the "Graph Cuts". In this scenario, the issue of segmentation is regarded the separation of an image into two classes "object" and "bottom". This approach for semi-automatic segmentation integrates some of the voxels of the volume to one of these two classes. This initial association acts then as base of training for the ultimate segmentation of the volume. This technique implements an energy minimization approach based on partitioning a graph into two sub-graphs by cutting minimum capacity.

Bae *et al.* [5] used simple thresholding and logic functions to attain the sketch of the liver before smoothing the boundary using B-splines. Gao *et al.* [3] extended the work through mathematical morphology on the threshold image to partition the liver from other organs, before refining the obtained contour with a Fourier-based deformable contour model. The drawback of both of these techniques is in the initial thresholding step where it is tough to set upper and lower threshold limits that separate the liver effectively, without taking into account the neighboring tissues such as the kidneys and the spleen. Thus, the initial starting point for the boundary refinement process is based on the inaccurate thresholding step.



Shimizu *et al.* [6] used the equivalent CT values from four different input images of the same liver to attain the rough contour. The main limitation of this approach is that four complete datasets are needed for effective segmentation of one liver. This needs four different CT scans of the same patient in succession, and computationally it requires four times the memory and processing power that is used when analyzing a single dataset. Computer-Aided Diagnosis (CAD) is being widely used to improve the interpretation components of medical imaging [7, 8]. Moreover, Computer-Aided Surgery (CAS) is carried out on computerized surgical planning and image-guided surgery by examining the Region-Of-Interest (ROI) in the medical image. Volume measurement is also of major significance in different fields of medical imaging where doctors need some assessments for surgical decisions.

Seoa multi-stage automatic hepatic tumor segmentation approach is presented [9]. It initially segments the liver, and eliminates hepatic vessels from the liver. Then, a hepatic tumor is segmented through the optimal threshold value with minimum total probability error. Active contour algorithm has been widely used in tumor segmentation. Yim *et al.* used watershed and active contour algorithms for volumetric investigation on ten hepatic metastatic lesions in 36 CT slices [10]. Lu *et al.* also used the active contour with aspecific initial contour to attain the tumor boundary [11]. Zhao *et al.* developed a region growing algorithm through intensity distributions of the seed ROI offered by users to delineate liver metastases. Particular shape constraints have been used to prevent the region growing from leaking into surrounding tissues [12]. But, there are certain drawbacks in the above said existing techniques. Most of the above said approaches segment the tumor in 2D. When considering CT volumetric data, segmentation is carried out slice by slice, and then the 2D results are integrated into a volume. Moreover, these techniques were tested on different data sets and evaluated using different standards. Hence it is difficult to compare their performance. To benchmark 3D liver tumor segmentation methods, the organizer of "3D Liver Tumor Segmentation Challenge 2008"[13] provided CT scans of livers from four patients with ten lesions manual segmented as training data, together with other six CT scans of livers with ten lesions (not segmented) as the testing data.



**Figure-1.** Segmentation of results.

Figure-1 Shows the segmentation process of the liver image. That perform the process of marked the region, then enhance the image after the do the segmentation process.

Hongwei *et al.* [14] presented an Auto-context Model (ACM) based automatic liver segmentation algorithm, which integrates ACM, multi-atlases and mean-shift techniques to segment liver from 3D CT images. This algorithm is learning based approach and can be categorized into two stages. At the initial training stage, ACM learns a series of classifiers in each atlas space. Through multiple atlases, multiple sequences of ACM-based classifiers are attained. In the second segmentation stage, the test image will be segmented in each atlas space through each sequence of ACM-based classifiers. The ultimate segmentation result will be attained by fusing segmentation results from all atlas spaces through a multi-classifier fusion approach. Even though ACM based liver segmentation is effective, it has some limitations:

- The features on the context information are still somewhat limited.
- Different auto-context models require to be trained for different applications.
- The algorithm is a supervised approach and thus needs a set of well-annotated ground truth data, which might not always be available or can be difficult to obtain.
- Method is a supervised learning technique, it needs a set of manual reference segmentations (ground-truth data), which is sometimes difficult to obtain.

The limitation of Mean-shift method is that, it is a time consuming image segmentation algorithm. In order to overcome these problems, kernel sparse coding segmentation algorithm is used for liver segmentation in the present research work.

## METHODOLOGY

The main contribution of the present research work is threefold. Initially, the pre processing is done followed by segmentation and classification. In segmentation we use kernel sparse coding for liver segmentation initially, dictionary design through kernel similarities, representation of test samples and finally discrimination of resultant codes.

Preprocessing the computed tomography images are preprocessed because of the high intensity between the liver tissue and adjacent organs, presence of several pathologies, varying shape of the liver. The normal segmentation algorithm is not enough for the best segmentation results because the edges of the liver are not clear and high intensities of the image. The preprocessing stage is used to overcome these problems by applying the filtering techniques such as Gaussian filter, sticks filter. In this paper, the combination of Laplacian filter and stick filter technique is used for better results and it removes the noises before the main segmentation. Stick filtering technique is one of the powerful techniques in image processing and filtering. It is mainly used for removing the



noise, image contrast and improves the boundaries of the liver. It is used for separating the liver image from adjacent organs by improving the boundaries. The second step of the proposed preprocessing technique is applying the laplacian filtering technique and it is mainly focused on the image intensity changes and used for improving the edges of the liver. In this paper it is combined with the stick filter for best results and the kernel of the Laplacian filter can be calculated as given equation.

$$LoG(x,y) = -\frac{1}{\pi\sigma^4} \left[ 1 - \frac{x^2+y^2}{2\sigma^2} \right] e^{-\frac{x^2+y^2}{2\sigma^2}} \quad (1)$$

Sparse Coding and Dictionary Learning Sparse models have been widely used in image analysis as several naturally occurring images can be efficiently formulated as a sparse linear combination of elementary features [15]. The elementary features are normalized to unit norm and stacked together to form the dictionary matrix. Given a sample  $y^M$ , and a dictionary  $\mathbb{R}^{M \times K}$  the generative model for sparse coding is given as  $Dx + n$ , where  $RK$  is the sparse code with a small number of non-zero coefficients and  $n$  is the noise component [16]. The sparse code can be computed by solving the convex problem

$$\min_x \|y - Dx\|_2^2 + \beta \|x\|_1 \quad (1)$$

Where  $\|x\|_1$  indicates the  $\ell_1$  norm, and is a convex surrogate for the  $\ell_0$  norm which counts the number of non-zero elements in a vector [17]. Some of the approaches used to solve (1) include the basis pursuit [18]; feature-sign search [19] and the least angle regression algorithm with the LASSO modification (LARS-LASSO) [20]. When presented with a adequately large set of training data samples,  $\{y^i\}_{i=1}^T$ , the dictionary can be learned, and the corresponding sparse codes can be obtained by solving equation (2).

$$\min_{D,x} \|Y - Dx\|_F^2 + \beta \sum_{i=1}^T \|x_i\|_1 \quad (2)$$

Where  $\{x_i\}_{i=1}^T$  and  $\|x_i\|_1$  denotes the Frobenius norm of the matrix. Equation (2) can be solved as an alternating minimization problem, where the dictionary is learned by fixing the sparse codes, and the sparse codes are obtained by fixing the dictionary. Dictionaries fixed to the data provide superior performance when compared to predefined dictionaries in a number of applications [21, 14]. Moreover, being valuable in data representation issues, there has been a recent surge of interest in using sparse models in several supervised, semi-supervised and unsupervised learning tasks such as clustering [22] and classification [23].

Kernel Sparse Coding for Liver Segmentation Sparse coding algorithms are mostly used for vectorized patches or feature vectors extracted from the images, through an over complete dictionary. It is typical in

machine learning techniques to utilize the kernel function to learn linear models in a feature space that captures the non-linear similarities. Kernel functions map the non-linear separable features into a feature space using a transformation  $\Phi$ , in which similar features are grouped together. By carrying out sparse coding in the feature space, highly discriminative codes can be obtained for samples from different classes [16, 24, and 25].

Kernel Sparse Coding with the feature mapping function  $\mathbb{R}^M \mapsto F$ , the generative model in  $F$  for kernel sparse coding is given by  $\Phi(D)x + n$ . The data sample  $y$  in the feature space is represented as  $\Phi(y)$  and the dictionary by  $\Phi(D) = [\Phi(d_1), \Phi(d_2), \dots, \Phi(d_k)]$ , the kernel similarities  $\langle y_i, y_j \rangle = \Phi(y_i)^T \Phi(y_j)$ ,  $K(d_k, y) = \Phi(d_k)^T \Phi(y)$  and  $\langle d_k, d_i \rangle = \Phi(d_k)^T \Phi(d_i)$  can be calculated through pre-defined kernel functions. All further computations in the feature space will be carried out exclusively using kernel similarities. The problem of sparse coding in (1) can be posed in the feature space as

$$\min_x \|\Phi(y) - \Phi(D)x\|_2^2 + \lambda \|x\|_1 \quad (3)$$

Expanding the objective in (3), the following equation is obtained

$$\begin{aligned} & \Phi(y)^T \Phi(y) - 2x^T \Phi(D)^T \Phi(y) + x^T \Phi(D)^T \Phi(D)x + \lambda \|x\|_1 \\ & = K_{yy} - 2x^T K_{Dy} + x^T K_{DD}x + \lambda \|x\|_1 \end{aligned} \quad (4)$$

denotes the element  $\langle y, y \rangle$ ,  $K_{Dy}$  is a  $K \times 1$  vector containing the elements  $\langle d_k, y \rangle, \forall k = \{1, \dots, K\}$  and  $K_{DD}$  is a  $K \times K$  matrix containing the kernel similarities between the dictionary atoms. The kernel sparse coding problem can be efficiently solved through the feature-sign search algorithm. However, it is essential that the computation of kernel matrices incurs additional complexity. As the dictionary is fixed in (4),  $K_{DD}$  denotes computed only once and the complexity of computing  $K_{DD}$  alters as  $\{K\}$ .

Kernel Dictionary Design Optimization of dictionaries in the feature space can be performed out by reposing the dictionary learning process through kernel similarities. These non-linear dictionaries provide compact representations, when compared to kernel PCA, and in modeling the non-linearity present in the training samples. The joint problem of dictionary learning and sparse coding is a generalization of 1-D subspace clustering [26]. In order to design the dictionary  $\Phi(D)$ , equation (2) is adapted to the feature space; with the constraint that only one element in the sparse code can be non-zero. This form of the kernel dictionary learning was proposed by Nguyen *et al* [27]. This is equivalent to the kernel version of K-lines clustering, which tries to fit  $K$  1-D subspaces to the training data in  $F$  [26]. Though sophisticated kernel dictionaries can be designed, utilizing dictionaries obtained using this simple clustering process results in



significant performance. The clustering problem can therefore be posed as

$$\min_{\mathbf{X}} \|\Phi(\mathbf{Y}) - (\mathbf{Y})\mathbf{A}\mathbf{X}\|_F^2 \text{ such that } \|x_i\|_0 \leq 1, \forall_i \quad (5)$$

Each dictionary atom  $\mathbf{d}_i$  is equivalent to a cluster center and each coefficient vector  $\mathbf{c}_i$  encodes the cluster association and the weight corresponding to the pixel. The alternating optimization for solving equation (5) consists of two steps: (a) cluster assignment, which involves finding the association and weight of each training vector and hence updating the sets  $\mathbf{C}_{k=1}^K$  and (b) cluster update, which involves updating the cluster center by finding the centroid of training vectors corresponding to each set  $\mathbf{C}_k$ .

In the cluster assignment step, the correlations of a training sample with the dictionary atoms can be formulated as  $\mathbf{c}_i^T \Phi(\mathbf{D}) = \mathbf{K}_{\mathbf{y}_i \mathbf{y}} \mathbf{A}$ . If the dictionary atom results in maximum absolute correlation, the index  $i$  is placed in set  $\mathbf{C}_k$ , and the corresponding non-zero coefficient is the correlation value itself. For the cluster  $k$  let  $\mathbf{c}_k = \Phi(\mathbf{Y})\mathbf{E}_k$  be the set of member vectors and  $\mathbf{a}_k$  be the row of corresponding non-zero weights. The cluster update involves solving the equation (6).

$$\min_{\mathbf{a}_k} \|\Phi(\mathbf{Y})\mathbf{a}_k \mathbf{x}_k^T - \Phi(\mathbf{Y})\mathbf{E}_k\|_F^2 \quad (6)$$

Denoting the singular value decomposition of

$$\Phi(\mathbf{Y}_k) = \mathbf{U}_k \Sigma_k \mathbf{V}_k^T \quad (7)$$

Rank-1 approximation, which also results in the optimal solution for equation (6), is given by

$$\Phi(\mathbf{Y})\mathbf{a}_k \mathbf{x}_k^T = \sigma_{k_1} \mathbf{u}_{k_1} \mathbf{v}_{k_1}^T \quad (8)$$

Where  $\sigma_{k_1}$  is the largest singular value, and  $\mathbf{u}_{k_1}$  and  $\mathbf{v}_{k_1}$  are the columns of  $\mathbf{U}_k$  and  $\mathbf{V}_k$  equivalent to that singular value. Equation (8) implies that  $\mathbf{a}_k = \mathbf{u}_{k_1}$  and  $\mathbf{x}_k = \sigma_{k_1}^{-1} \mathbf{v}_{k_1}^T$ . Let the Eigen decomposition of  $\mathbf{V}_k$  be  $\mathbf{V}_k = \mathbf{Q}_k \mathbf{\Lambda}_k \mathbf{Q}_k^T$  and hence  $\mathbf{x}_k = \mathbf{Q}_k \mathbf{\Lambda}_k^{-1} \mathbf{1}$  assuming the Eigen values are in descending order. From equation (7),  $\mathbf{c}_k = \sigma_{k_1} \mathbf{u}_{k_1}$ . Substituting for  $\mathbf{c}_k$  and  $\mathbf{a}_k = \mathbf{u}_{k_1}$  and  $\mathbf{x}_k = \sigma_{k_1}^{-1} \mathbf{Q}_k \mathbf{\Lambda}_k^{-1} \mathbf{1}$  is obtained which results in

$$\mathbf{a}_k = \sigma_{k_1}^{-1} \mathbf{E}_k \mathbf{v}_{k_1} \quad (9)$$

Note that  $\mathbf{a}_k$  completely defines  $\mathbf{c}_k$ . The cluster assignment and update steps are repeated until convergence, i.e., when  $\{\mathbf{C}_k\}_{k=1}^K$  does not change over iterations.

Representation Kernel sparse coding is used as an alternative to techniques such as kernel PCA for efficient data representation. Though, entire reconstruction of the

fundamental data from the kernel sparse codes need computation of pre-images [28], novel test samples can also be well approximated using the learned kernel dictionaries.

Discrimination Kernel sparse coding is well suited for supervised learning tasks. As the non-linear similarities between the training samples are taken into consideration while learning the dictionary, the resulting codes are highly discriminative. The kernel sparse codes are obtained for all the samples and the normalized cross correlation are computed between the sparse features. As kernel sparse codes promote discrimination, features belonging to a class are expected to be highly similar when compared with the samples from other classes.

### PROPOSED ALGORITHM

The proposed algorithm is used for liver segmentation using Kernel Sparse Coding-Based Automated (KSCA) segmentation algorithm. In the algorithm the training set of images are taken which is used for aligning and segmentation purpose although the segmentation is unendorsed learning here we consider it as proven. The Kernel Matrix is generated through pixel intensities and spatial locations and the kernel dictionaries are attained based on kernel dictionary optimization and kernel sparse coding for sparse coding pixels in nonlinear feature space. The images are partitioned into  $K$  subsets by using  $K$ -line clustering algorithm along with the help of kernel sparse dictionary learning. The output of the clustering procedure sparse code trains the ELM classifier which is used to find the affected regions of the liver based on the pixel.

Combining Multiple Features When compared to using a single feature, using multiple features to characterize images has been a very successful approach for classification tasks. Though this method provides the flexibility of choosing features to describe different aspects of the underlying data, the result and illustrations are high-dimensional and the descriptors could be varied diversely. Therefore, there is a need to transform the features to a unified space that allows the recognition functions, and generate low dimensional compact representations for the images in the unified space. A set of  $R$  diverse descriptors are extracted from a given image. As the kernel similarities can be utilized to fuse the multiple descriptors, the base kernel matrix is constructed for each descriptor. A suitable distance function is given which evaluates the distance between two samples for the feature the kernel matrix can be constructed as

$$K_r(\mathbf{Y}_i, \mathbf{Y}_j) = \exp(-\gamma d_r^2(\mathbf{Y}_i, \mathbf{Y}_j)) \quad (10)$$

Where  $\gamma$  is a positive constant? Given the  $R$  base kernel matrices,  $\mathbf{K}_{r=1}^R$ , we can construct the ensemble kernel matrix as

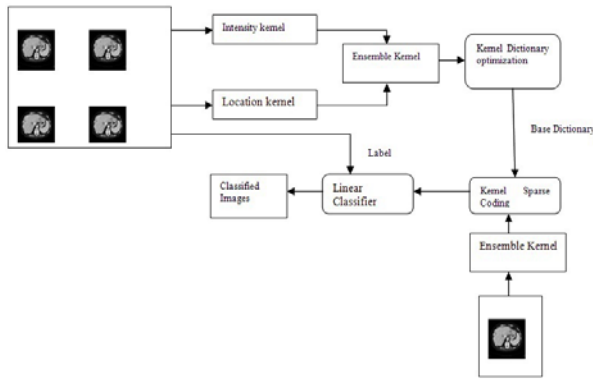
$$\mathbf{K} = \sum_{r=1}^R \beta_r \mathbf{K}_r, \quad \forall \beta_r \geq 0 \quad (11)$$



A constructive alternate technique to fuse the descriptors is to attain the ensemble kernel matrix as

$$K = K_1 \circ K_2 \circ K_3 \dots \circ K_L \tag{12}$$

Where  $\circ$  denotes the Hadamard product between two matrices. Sparse codes calculated with the ensemble kernel matrices will take all the R features into consideration. Note that when combining kernel matrices, we need to ensure that the resulting kernel matrix also satisfies the Mercer's conditions.



**Figure-2.** The figure depicts the proposed algorithm for automated liver segmentation.

Figure-2 Shows For a set of training samples, the ensemble kernel dictionary is obtained using Kernel K-lines clustering procedure and ELM classifier is used to classify the pixels.4.2. Algorithm

The proposed algorithm of this research work is Kernel Sparse Coding-based Automated (KSCA) segmentation algorithm. The kernel matrix  $K \in \mathbb{R}^{T \times T}$  is computed using RBF kernel on pixel intensity values for the subset of pixels T. in order obtain the ensemble kernel matrix, the fusion of intensity and spatial location matrix is take place.

$$K = K_I \circ K_L \tag{13}$$

The sparse codes attained with a dictionary learned in the ensemble feature space model the similarities of pixels according to both intensity and location of pixels. A group of training images, with active tumor regions, are utilized to learn a kernel dictionary with the kernel K-lines clustering process. Using the kernel sparse codes belonging to affected and non-affected regions, ELM classifier is used to classify the affected regions based on the pixel. For a test image, the required ensemble kernel matrices are obtained and the kernel sparse codes using the learned dictionary are computed.

**ELM Description**

ELM is a unified Single hidden Layer Feed forward Neural network (SLFN) with randomly generated

hidden nodes independent of the training data [29, 30]. For N arbitrary distinct samples  $x_i$  where  $x_i = [x_{i1}, x_{i2}, \dots, x_{im}]^T \in \mathbb{R}^m$  and  $[t_{i1}, t_{i2}, \dots, t_{im}]^T \in \mathbb{R}^m$  (n is the number of dimensions of input x, m is the number of classes of data). So a given set of training samples  $\{x_i, t_i\}_{i=1}^N \subset \mathbb{R}^n \times \mathbb{R}^m$  the output of a SLFN with L hidden nodes can be represented by

$$y_j = \sum_{i=1}^L \beta_i K(\alpha_i, b_i, x_j) = t_j, j = 1 \dots N \tag{14}$$

where  $\alpha_i$  and  $b_i$  are the parameters of hidden node which could be randomly generated.  $K(\alpha_i, b_i, x)$  is the output of the hidden node with respect to the input x. And  $\beta_i$  is the weight connecting the hidden node to the output node. Equation (1) can be written compactly as

$$H\beta = T \tag{15}$$

$$H = \begin{bmatrix} K(\alpha_1, b_1, x_1) & \dots & K(\alpha_L, b_L, x_1) \\ \vdots & \ddots & \vdots \\ K(\alpha_1, b_1, x_N) & \dots & K(\alpha_L, b_L, x_N) \end{bmatrix}$$

$$\beta = \begin{bmatrix} \beta_1^T \\ \vdots \\ \beta_L^T \end{bmatrix} \quad \text{and} \quad T = \begin{bmatrix} t_1^T \\ \vdots \\ t_N^T \end{bmatrix}$$

is the transpose of a matrix or vector. H is called the hidden layer output matrix of the network [30]; the column of H is the hidden node's output vector with respect to inputs  $x_1, \dots, x_N$ ; and the row of H is the output vector of the hidden layer with respect to input  $x_i$ . It has been proved in theory [29, 30] that SLFNs with random hidden nodes have the universal approximation capability, and the hidden nodes can be randomly generated independent of the training data.

After the hidden nodes are randomly generated and given the training data, the hidden-layer output matrix H is known and need not be tuned. Thus, training SLFNs simply amounts to getting the solution of a linear system (2) of output weights according to Bartlett's theory [30] for feed forward neural networks, in order to get the better generalization performance, ELM not only tries to reach the smallest training error but also the smallest norm of output weights.

**Minimize:**  $\|H\beta - T\|$

And

**Minimize:**  $\|\beta\|$

In the case of binary classification, Huang *et al.* [31] proved that to minimize the norm of the output weights  $\beta$  is actually to maximize the distance of the separating margins of the two different classes  $2 = \beta^T k \beta$  in ELM feature space.



Under the constraint of equation (5), a simple representation of the solution of the system (2) is given explicitly by Huang *et al.* [31] as

$$H^\dagger T \quad (16)$$

Where the Moore-Penrose is generalized inverse of the hidden-layer output matrix  $H$ . If the  $N$  training data are distinct,  $H$  is column full rank with high probability when  $N$ . In real applications, the number of hidden nodes is always less than the number of training data  $N$ . Thus

$$H^\dagger = (H^T H)^{-1} H^T \quad (17)$$

Huang *et al.* [31] have proved SLFNs with a wide type of random computational hidden nodes. Additive and RBF hidden nodes are used often in applications. For example, additive hidden node with the activation function  $f: R \rightarrow R$  (e.g., sigmoid, threshold, sin/cos, etc.),  $\langle a_i, b_i, x \rangle$  is given by

$$K(a_i, b_i, x) = K(a_i, x + b_i) \quad (18)$$

Where  $\alpha$  is the weight vector connecting the input layer to the hidden node and  $b$  is the bias of the hidden node.  $\langle a, x \rangle$  denotes the inner product of vectors  $a$  and  $x$  in  $R^n$ . The three-step simple learning algorithm can be summarized as follows:

#### Algorithm 1

Given a training set  $\{t_i\}_{i=1}^N \subset R^n \times R^m$ , the hidden-node output function  $f(a_i, b_i, x)$  and hidden-node number  $L$ :

Step 1: Randomly assign hidden-node parameters

$$b_i, i = 1, \dots, L$$

Step 2: Calculate the hidden-layer output matrix  $H$ ;

Step 3: Calculate the output weight vector  $T = H^\dagger T$

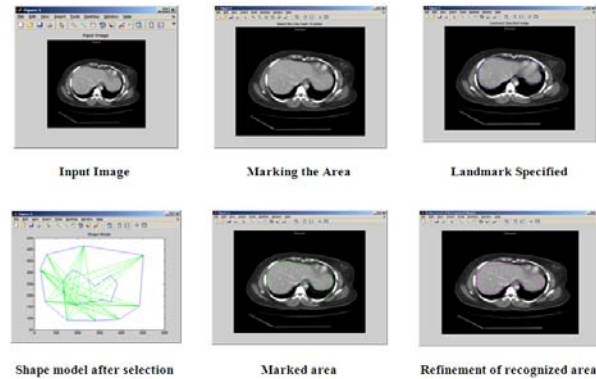
In this paper ELM is used as classifier to identify the pixels belonging to affected region of liver.

## EXPERIMENTS

The results are compared to manual segmentations performed by a radio-oncology specialist, based on both the subjective visual quality and quantitative standards such as Accuracy (Acc) and Correspondence Ratio (CR). The learning-based liver segmentation technique is evaluated based on the training and testing datasets of MICCAI 2007 liver segmentation challenge (<http://www.sliver07.org>). There are 20 contrast-enhanced abdominal CT images in the training datasets and 10 in the testing datasets. All images have a spatial resolution of  $512 \times 512$  pixels in each transversal slice and the pixel spacing varies from 0.55 to 0.9mm. The inter-slice distance varies from 0.5 to 5mm. In this paper, 10 CT images from the training datasets (denoted as "TrainIM") are randomly chosen for learning.

The remaining 10 CT images in the training datasets (represented as "TestIM1") and 10 CT images in the testing datasets (represented as "TestIM2") are used

for evaluation. The MICCAI 2007 workshop provides manual liver labels only for the training datasets, not for the testing datasets. Thus do "TestIM1" for quantitative evaluation and then both "TestIM1" and "TestIM2" for equality evaluation.



**Figure-3.** Liver segmentation using Kernel sparse coding based automated segmentation algorithm.

In this Figure the input image is procured from the testing datasets and a precise area is blotted. Now the discernible location is stipulated with a landmark and a new shape model is being engendered in a graphical genre. This graphic sculpt is then employed to augment the renowned area.

## RESULT

Simulations are executed for both the semi-automated and automated algorithms for every axial slice. For both of the proposed algorithms, the parameter  $\gamma$  for the RBF kernel was set to 0.3, and the dictionary size was fixed at 256. In the automated approach, the ensemble kernel is evaluated for 15, 000 randomly chosen pixels from the training set. The performance of the proposed approach is compared based on metrics such as Accuracy (Acc) and Correspondence Ratio (CR) computed as [34].

$$Acc = \frac{TP}{Total\# \text{ affected pixels in the GT image}} \quad (19)$$

And

$$CR = \frac{TP - 0.5FP}{Total\# \text{ affected pixels in the GT image}} \quad (20)$$

Where TP indicates the number of true positives (the pixels indicated as affected regions by the ground truth and our algorithm), and FP represents the number of false positives (pixels indicated as non-affected by the ground truth, but affected by this algorithm).

**Table-1.** Performance evaluation comparison.

Method	OE (%)	SVD (%)	DAvg (MM)	Drms (MM)	Dmax (MM)	Runtime (sec)	Accuracy (%)
Heiman	7.7	1.7	1.4	3.2	30.1	7	70
Zhang	5.3	0.7	0.9	2.2	24.8	NA	74
ACM+multi-atlas	7.5	2.1	1.3	3.1	28.8	39.5	79
ACM+multi-atlas+mean-shift	8.3	2.7	1.5	3.1	29.3	35	82
<b>Proposed Kernel sparse coding</b>	<b>5</b>	<b>1.1</b>	<b>0.8</b>	<b>2</b>	<b>25</b>	<b>33</b>	<b>91</b>

Table-1 shows the performance comparison of the proposed Kernel sparse coding based Automated Segmentation algorithm with other existing algorithms such as Heiman's approach [33], Zhang's approach [34], ACM multi-atlas approach and ACM multi-atlas with mean-shift approach [35].

The parameters taken for consideration are volumetric Overlap Error (OE) in percentage, Signed relative Volume Difference (SVD) in percentage, Average symmetric surface Distance (DAvg) in (MM), Root Mean Square symmetric surface distance (DRMS) and Maximum symmetric Surface Distance (DMax), run time in minutes and the Accuracy of the image.

**Volumetric Overlap Error (OE) (percent):** This is the quantity of voxels in the meeting point of segmentation and reference divided by the number of voxels in the combination of segmentation and reference, subtracted from 1 and multiplied by 100. Relative absolute volume difference (percent): The total volume difference of the segmentation to the reference is separated by the entire quantity of the reference. The result is multiplied by 100. This signed number is reported in the Tables of the papers in these proceedings, so one can recognize under segmentations by negative values and over segmentation by positive values. To compute a score, the absolute value is taken.

**Average symmetric surface distance (millimeters):** The border voxels of segmentation and reference are determined. These are defined as those voxels in the object that have at least one neighbor (of their 18 nearest neighbors) that does not fit into the object. For each voxel along one border, the closest voxel along the other border is determined using Euclidean distance, not signed, and real world distances. All these distances are accumulated, for border voxels from both reference and segmentation. The average of all these distances gives the average symmetric absolute surface distance. This value is 0 for a perfect segmentation.

**Root Mean Square (RMS) symmetric surface distance (millimeters):** This measure is similar to the previous measure, but stores the squared distances between the two sets of order voxels. Subsequent to averaging the squared values, the root is extracted to give the symmetric RMS surface distance.

**Maximum symmetric surface distance (millimeters):** This measure is similar to the previous two, but in this case the maximum of all voxel distances is

taken as an alternative to the average. This rate is 0 for a perfect segmentation.

Table-1 clearly indicates that the proposed Kernel sparse coding based Automated Segmentation algorithm provides significant results when compared with the other existing approaches taken into consideration.

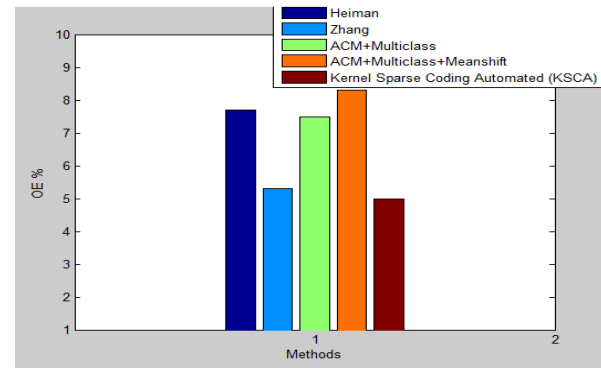
**Figure-4.** OE graph for proposed approach.

Figure-4 shows the OE comparison of the proposed Kernel sparse coding approach and the existing approaches such as Heiman, Zhang, ACM+multi-atlas and ACM+multi-atlas+mean-shift. It is observed that the proposed approach attains 5% OE, whereas the other approaches attain higher values than proposed approach.

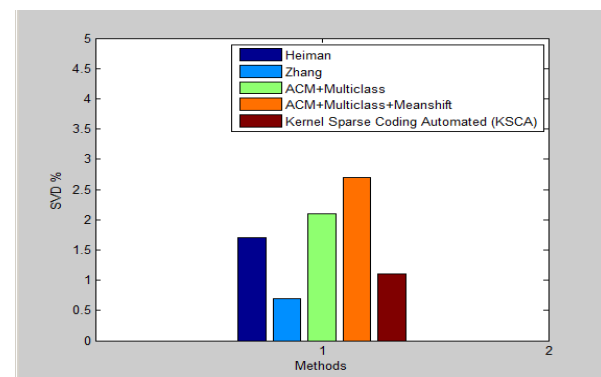
**Figure-5.** SVD comparison.

Figure-5 shows the SVD comparison graph. The SVD value attained by the proposed Kernel sparse coding approach is 2.8% whereas the existing approaches such as Heiman, Zhang, ACM+multi-atlas and ACM+multi-atlas+mean-shift attains the SVD values of 1.7%, 0.7%, 2.1% and 2.7% respectively. Thus the proposed approach outperforms the other approaches.

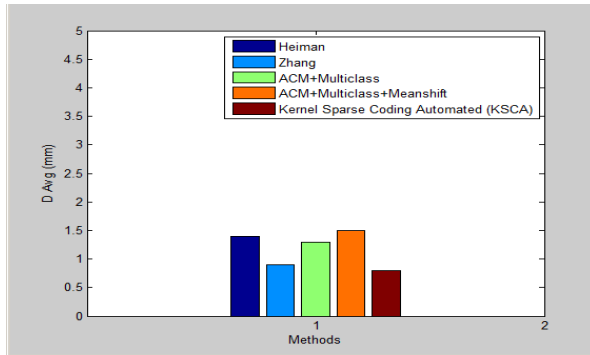


Figure-6. D Avg comparison.

DAvg comparison is shown in Figure-6. It is observed from the Figure that the proposed Kernel sparse coding approach attains 2% D Avg whereas the existing approaches such as Heiman, Zhang, ACM+multi-atlas and ACM+multi-atlas+mean-shift attains the D Avg values of 1.4%, 0.9%, 1.3% and 1.5% respectively. Thus the proposed approach outperforms the other approaches.

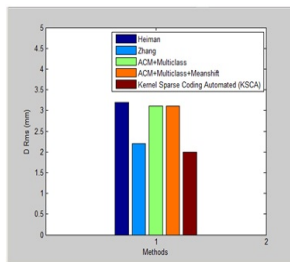


Figure-7. Drms comparison

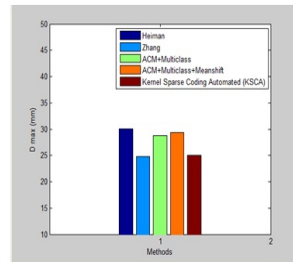


Figure-8. D-max Comparison.

Figure 7 and 8 shows the performance comparison of the Drms and D-max. It is clearly observed from the results that the proposed approach outperforms the existing approaches in terms of Drms and D-max. The values of Drms and D-max of the proposed kernel sparse approach is 2 MM and 25 MM, respectively which is lower than the existing approaches.

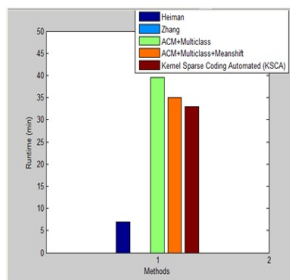


Figure-9. Runtime comparison.

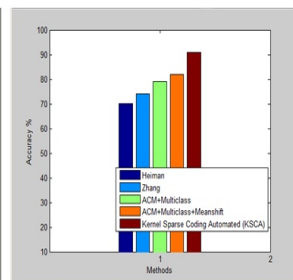


Figure 10. Accuracy comparison.

Figures 9 and 10 show the performance comparison of runtime and accuracy for different

approaches. It is observed from the Figures that the proposed Kernel sparse coding approach attains 91% accuracy whereas the existing approaches such as Heiman, Zhang, ACM+multi-atlas and ACM+multi-atlas+mean-shift attains the accuracy of 70%, 74%, 79% and 82% respectively. Thus the proposed approach outperforms the other approaches. The run time taken by the proposed kernel sparse coding approach is lower than ACM multi-atlas mean shift approach. This research work performs fairly in terms of runtime. The future work is to lessen the time consumed by the proposed approach.

## CONCLUSIONS

Accurate segmentation of liver tissue from medical images has become an active area of research in medical image processing. This research work aims to develop an efficient liver segmentation approach for computer aided liver disease diagnosis and surgical planning. This paper proposes an efficient kernel sparse coding approach for liver segmentation. The two metrics are used to construct kernel matrices they are pixel intensities and their spatial locations. The intensity matrix and spatial location matrix are combined to construct the ensemble kernel matrix. The kernel dictionary for sparse coding pixels in a nonlinear feature space is also obtained from the kernel matrix. The linear classifier is used to classify the affected regions in the liver. The experimental result shows that the proposed kernel sparse coding technique performs better than other liver segmentation techniques such as Heimen, Zhang, ACM+Multiclass and ACM+Multiclass+Meanshift approach.

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